## Introduction to Computer Graphics

#### Marie-Paule Cani & Estelle Duveau

```
04/02 Introduction & projective rendering
11/02 Prodedural modeling, Interactive modeling with parametric surfaces
25/02 Introduction to OpenGL + lab: first steps & modeling
04/03 Implicit surfaces 1
                               + lecture/lab: transformations & hierarchies
11/03 Implicit surfaces 2 + Lights & materials in OpenGL
18/03 Textures, aliasing
                             + Lab: Lights & materials in OpenGL
25/03 Textures in OpenGL: lecture + lab
01/04 Procedural & kinematic animation + lab: procedural anim
08/04 Physically-based animation: particle systems + lab: physics 1
22/04 Physically-based animation: collisions, control + lab: physics 2
29/04 Animating complex objects + Realistic rendering
06/05 Talks: results of cases studies
```

## Descriptive vs Procedural animation

#### Descriptive animation

Describes a single motion

Ex: interpolating key-frames, direct and inverse kinematics

#### Procedural animation

Generates a familly of motion and deformations from

- Initial conditions
- Laws of motion
- Interaction (from other objects or the user)

Ex: physically-based models

### Physically-based models

#### Laws of motion from mecanics

• Model + intial conditions + applied forces → motion

### Advantage: a help for realism!

- useful when dynamics plays an important part
- easier for passive models!

### Examples:

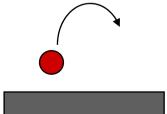
- Toy-Story 1, Shreck



## Physically-based models

### Animation algorithm

- At each time step
  - for each object
    - 1. Compute new speed (use its law of motion)
    - 2. Compute new position
    - 3. Detect collisions *not so simple!*
    - 4. Update geometry
    - 5. Update applied forces

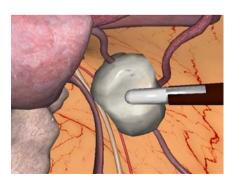


## Physically-based models Which law do we need?













## Physically-based models Which law do we need?

- Physically-based particles
  - Gravels, sand, ...
- Solids
- Articulated solids

### Examples:

- Rolling ball?
- Lamps?
- Wire?









## Physically-based models Which law do we need?

### Structured deformations

- Elasticity
  - Deformation function of constraints
  - Back to equilibrium
- Visco-elasticity
  - Speed of deformation
- Fractures

Ex : ball, flag, organ

### Un-structured

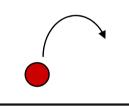
- Neighbors change!
- Plasticity
  - Absorbs deformations
- Fluids
  - Navier-Stockes

Ex: modeling clay, liquids, smoke and clouds...

## Some physical laws

#### **Points**

- Model / m, X, V /
- Law:  $F = \sum forces = m \ a$



#### Solids

- Model [m, I inertia matrix, X, V, rotation  $\omega$ ,  $\dot{\omega}$ ]
- Laws:  $\sum F = m \ a$

$$\sum M = I \dot{\omega} + \omega \wedge I \omega$$

Difficulty: representation of orientations!



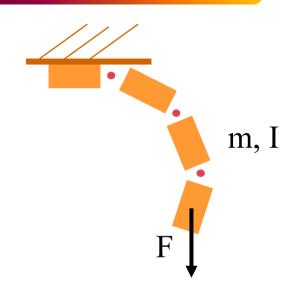
## Some physical laws

#### Articulated solids

Solid dynamics + constraints at joints!
 (Lagrange multipliers..)

### Deformable models

- Linear vs non-linear elasticity
- Navier stokes for fluids
   Eulerian vs Lagrangian discretization





### Example: Visco-elastic models

- Cauchy: linear deformation law
- OK for small displacements
- but rotations produce forces!
- the object inflates!!

## Apply Cauchy in local frames! [Müller et al. 02, 04]

- similar to Green's non-linear tensor
- real-time





## Example: Animating fratures

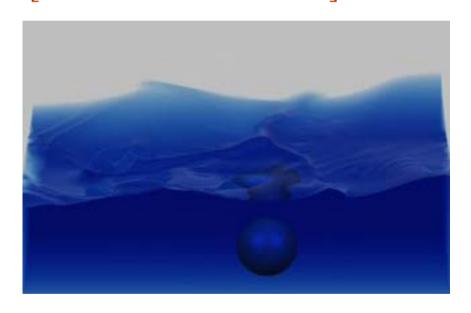
[James O'Brien]



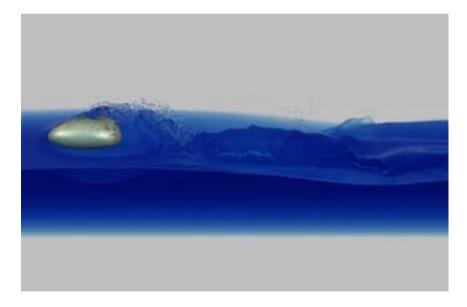
## Example: liquids

Navier stockes +Eulerian grid +"level set" (implicit)

#### [Foster & Fedkiw 2001]



#### [Enright et al. 2002]



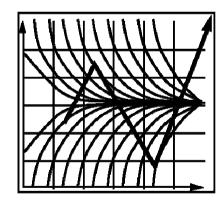
## Be careful with integration!

$$\ddot{\mathbf{x}} = F(\dot{\mathbf{x}}, \mathbf{x}, t) = \mathbf{f} / m$$
  
 $\dot{\mathbf{x}} = \mathbf{v}$ 

$$\dot{\mathbf{v}} = F(\mathbf{v}, \mathbf{x}, t)$$

• Explicit Euler

$$\mathbf{v}(t + \Delta t) = \mathbf{v}(t) + \Delta t F(\mathbf{v}(t), \mathbf{x}(t), t)$$
$$\mathbf{x}(t + \Delta t) = \mathbf{x}(t) + \Delta t \mathbf{v}(t)$$



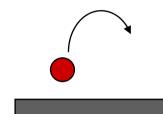
• Implicit Euler (much more stable!)

$$\mathbf{v}(t + \Delta t) = \mathbf{v}(t) + \Delta t F(\mathbf{v}(t + \Delta t), \mathbf{x}(t + \Delta t), t)$$

$$\mathbf{x}(t + \Delta t) = \mathbf{x}(t) + \Delta t \mathbf{v}(t + \Delta t)$$

## Do it all with point-based physics?

- Model: Particles [ m, X, V ]
- Point-based physics  $\sum forces = m \ a$ Animation algorithm



At each time step, for each particle

$$V(t+dt) = V(t) + \sum F(t)/m dt$$

$$X(t+dt) = xX(t) + V(t) dt \text{ (if explicit Euler)}$$

- Adapted forces?
- Render with adapted geometry!

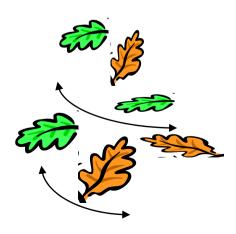


## Do it all with point-based physics? Lots of simple objects

### "Physically-based particle systems"

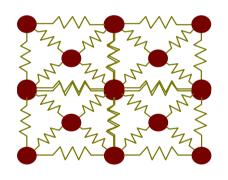
- Example : gravels, cereals
  - Gravity
  - Spheres for collisions detection
  - Random individual geometry
- Example : animating automn
  - Leaves = particle + local frame
  - Wind primitives
  - Gravity
  - Directional friction force

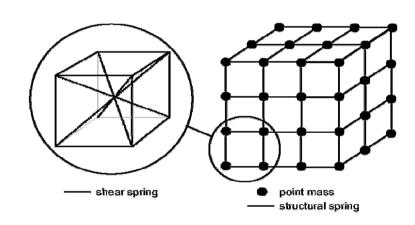




## Do it all with point-based physics? Stuctured material

• 1D, 2D, 3D mass-spring networks







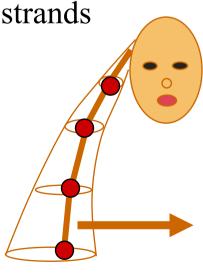
- Rigid and articulated solids?
  - Doable but very stiff! Too small time steps!

### Example 1D case: hair animation

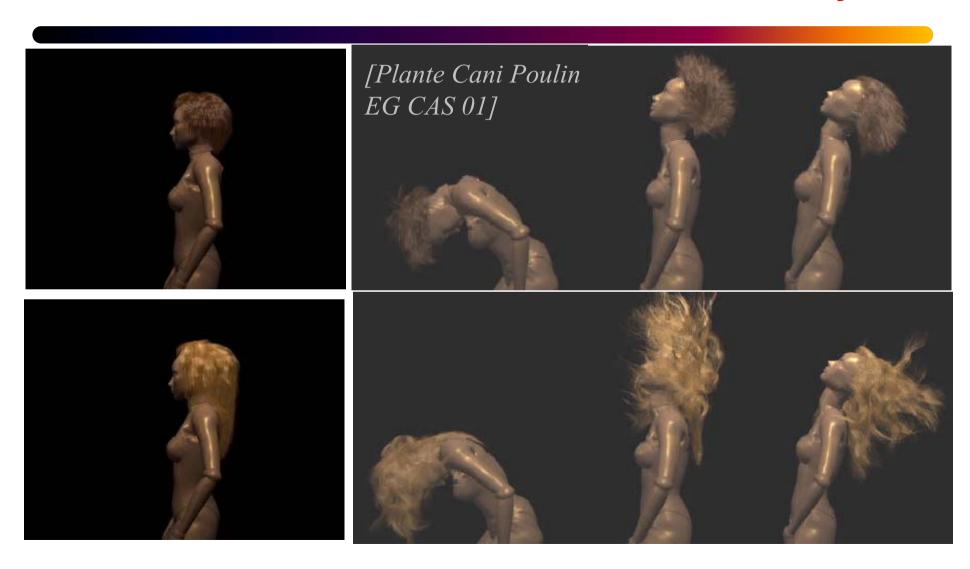
- Dynamics, inertia: wisp skeleton = chain of masses and springs
- Deformable wisp: add radial springs
- Anisotropic collisions

Render individual hair strands

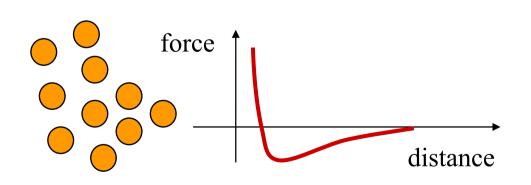


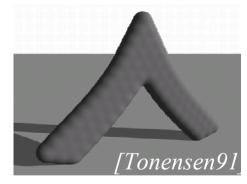


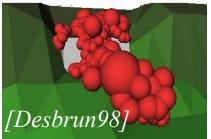




- Particle systems inspired from molecular dynamics
  - Lennard-Jones attraction/repulsion forces

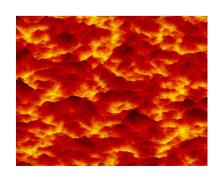


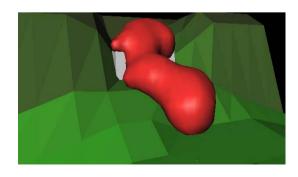


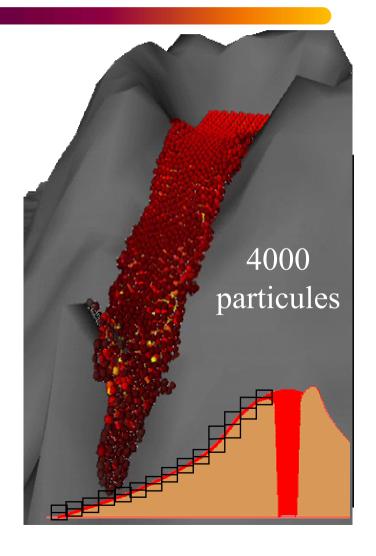


### Example: Lava flow

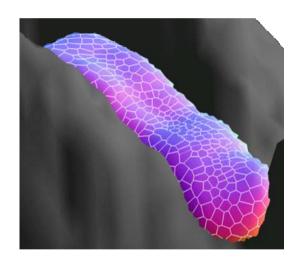
- SPH particles + temperature
- Heat-diffusion equation
- Render with an implicit surface
- Generate crust texture
   Animated Perlin noise

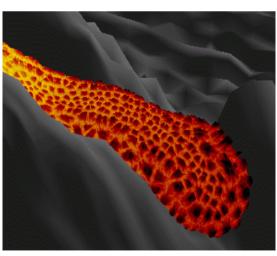


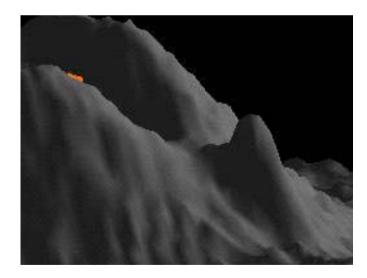




Lava flows: Coupling particles and crust [Stora Agliati Cani Neyret 99]

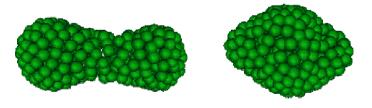


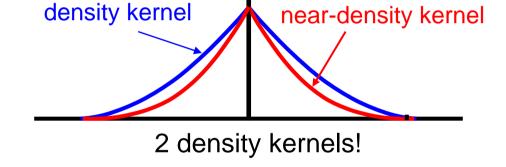




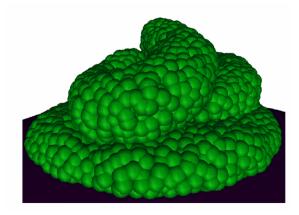
### Viscous fluids in real-time [Clavet, Beaudoin, Poulin, SCA'2005]

- Particules SPH :  $P = \rho \rho_0$
- Surface tension effect





- Real-time for 1500 particles
- Plasticity: add/remove springs



## Particle-based Viscoelastic Fluid Simulation

Simon Clavet
Philippe Beaudoin
Pierre Poulin

**SCA 2005** 

Bi-phasic fluids
with vortex particles
[Coquerelle, Cottet, Cani 2006]

Cup Falling, Camera Up

100 x 100 x 100 100 steps / s