

### PROGRAMME JEUNES CHERCHEUSES ET JEUNES CHERCHEURS

### EDITION 2010

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Titre du projet en anglais		Scalable Interactive Models Of Nature on Earth		
Comité d'Evaluation référence (CE) <sup>1</sup>		SIMI 2		
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<sup>&</sup>lt;sup>1</sup> Indiquer la référence du CE choisi pour l'évaluation du projet (cf. tableaux page 3 et 4 du texte de l'appel à projets)

# **1.** CONTEXTE ET POSITIONNEMENT DU PROJET / CONTEXT AND POSITIONNING OF THE PROPOSAL

The overall goal of the project is to provide representations and algorithms for the real-time navigation, on consumer hardware, in a realistic and plausible **virtual Earth model**. We target the rendering of terrain, vegetation, water surfaces and clouds (we exclude human artefacts), all highly detailed at all scales from ground to space, with physically based motion and illumination at all scales, and without visible transitions between scales. We do *not* target the best possible physical accuracy as in radiative transfer models or computational fluid dynamics methods (like for instance in remote sensing, climate modelization, meteorology, etc). Instead, we target physical *plausibility*, i.e., shape, illumination and motion models that *look* realistic and are efficient enough for real-time applications. Our main goals are:

- Scalability: we want to show a virtual Earth at scales varying between millimeters and thousands of kilometers. In this context storing, transferring, computing, rendering, simulating and controlling 3D models are all fundamentally impacted. The representation of the shape, of the motion and of the illumination of objects must be adapted with scale. For instance multi-scale physical models of light transport for terrains, vegetation, water surfaces and clouds are required, as well as multi-scale physical models of motion for ocean waves and clouds.
- Visual quality and realism: we target not only physically plausible and detailed shape, motion and illumination of all elements at all scales, but also seamless transitions between scales.
- **Real-time** performance on consumer hardware: this is required for most applications of a virtual Earth model, movies excepted.

Many international companies and actors are competing in this field, including Google (Google Earth), Microsoft (Bing Maps 3D, Flight Simulator X), Nasa (Nasa WorldWind), Crytex (Crysis). Several French companies and actors are also present in this field, including IGN (Geoportail), RSACosmos (planetariums), VWorld (virtual globe). Several research projects also addressed parts of the problem (including ANR projects like Vertigo, Prodige and Natsim - see next section for details). However, no existing products or research results can fully achieve the above goals. Indeed, existing products and research results either:

- don't target real-time performance: this is the case for movie special effects, and for synthetic world builders like Terragen, MojoWorld, Bryce, and Vue d'Esprit.
- limit the navigation area: for instance recent games such as Crysis achieve very realistic renderings in real-time. But they restrict players to move on a small area (missions or levels of a few square kilometers), and often to stay at the ground level.
- limit the amount of details: many applications provide details at only one scale. For instance flight simulators do not provide many details for ground views outside airports.
- don't target or achieve realism: 3D maps applications like Google Earth, Nasa WorldWind and Geoportail use unrealistic illumination models for the terrain, the atmosphere or clouds. The lack of vegetation is also unrealistic. Even applications targeting realism (such as Celestia, a virtual Universe model including a virtual Earth) do not provide fully realistic illumination models, due to real-time constraints.
- don't target animated elements like water and clouds.

Hence, applications that could benefit from the scientific breakthroughs we want to address are numerous: 3D maps such as Goole Earth, simulators for planes, boats, trains or cars, video games, impact studies, virtual Earth model for planetariums, enriched meteo presentation, etc.

# 2. DESCRIPTION SCIENTIFIQUE ET TECHNIQUE / SCIENTIFIC AND TECHNICAL DESCRIPTION

### 2.1. ÉTAT DE L'ART / BACKGROUND, STATE OF ART

### 2.1.1 STATE OF THE ART IN INDUSTRY

Numerous tools used for movies like Avatar, and dedicated world builder products (Terragen, Vue d'Esprit, MojoWorld, Bryce, etc) can generate large and detailed virtual worlds. But they do not target real-time at all: rendering complex scenes requires hours, several orders of magnitude more than the tens of milliseconds required for real-time.

Video games like Fuel and Crysis (probably the state of art in its domain) display very realistic outdoor environments in real-time. In Crysis the player can navigate in real-time in a whole island with highly detailed and realistic terrain, vegetation, waving and flowing water. However, transitions artifacts are visible between levels of detail (both on shape and illumination), flowing water and clouds are not very realistic, ocean waves are limited to the shore, and the whole environment is restricted to a few square kilometers (ten thousands for Fuel, but with less details). Outside this domain (for example in the associated game level editor, where users can move anywhere, at any speed) visible transitions between levels of detail become very visible.

Many civil, military and game simulators exists for planes, boats, trains and cars (Thales TSS, Corys, Flight Simulator X, Need for Speed, etc). They generally limit the environment to a given area, (except for flight simulators). When foreground details are provided, rough levels of detail are generally used, showing transition artifacts between levels (objects commonly appear suddenly when the user is close enough). Clouds are not 3D and the most realistic ones are not evolving and are not realistically illuminated (even in flight simulators).

3D maps applications like Google Earth, Bing Maps 3D, Nasa WorldWind and Geoportail display a virtual Earth model in real-time, at all scales from ground to space. They are highly scalable and can display many kind of geographic data. However, the transitions between level of details are very visible (new details appear suddenly when they have been downloaded over the network). Although details as small as 50cm can be visible, they are simply projected on the 3D terrain (which is much less detailed), giving a flat unnatural look in perspective views. No vegetation or other 3D details are provided at ground level, except coarse buildings in some areas. Overhangs and arches are an issue. Ocean, clouds and the atmosphere are displayed with a very basic shading that does not look realistic.

In summary, applications providing highly realistic renderings are restricted to small domains and limited user movements, while those providing full navigation capabilities suffer from rendering and animation problems. There is not currently a virtual Earth model with real-time highly realistic rendering and animation, where users are free to move and look anywhere. This is due to several scientific locks that we want to address in this project. Such a virtual Earth model would be useful for more realistic Earth browsers and flight simulators, and for realistic games on very large terrains with unrestricted users movements.

#### 2.1.2 State of the art in academic research

Our goals in this project pose several **scientific challenges**. These challenges are linked to the need for shape, motion and illumination models that can scale seamlessly from millimeters to thousands of kilometers. We recall here that we do *not* target the best possible physical accuracy as in radiative transfer models or computational fluid dynamics methods (like for instance in remote sensing, climate modelization, meteorology, etc). Instead, we target physical *plausibility*, i.e., shape, illumination and motion models that *look* realistic and are efficient enough for real-time applications. This is a different but equally challenging problem.

Scalable shape models. Some shapes must be reproduced with high accuracy (like the Earth topography), while others can be plausible without being exact, like vegetation, water waves, clouds, etc. The first ones require mass of data that largely exceed the computer or graphics card memory. Many representation, compression, storage, loading and streaming techniques have been proposed to extract on the fly the data for a given viewpoint, from a huge but slow storage. The terrain specific algorithms [PH93, Paj98, DWS+97, LH04, AH05, GMC+06] are now mature and provide continuous transitions between the discrete levels of detail (using morphing, still visible on silhouettes). Shapes that can be plausible without being exact can be generated on the fly from a small number of parameters and prior knowledge, using procedural techniques [EMP+94]. Several algorithms using fractals, L-systems, noise functions, point distributions, etc have been proposed for terrains [LH04], grass [GPR+03, SKP05, BPB09], plants and trees [WP95, DCSD02], plant distributions [DHL+98, LP02, AM09], forests [DN04, FMU05], clouds [HL01, NDN96, Ney97, REK+04, BNL06, BNM+08], etc. The first challenge is to provide scalability: many algorithms address only one scale (e.g., an individual tree or a forest, an individual cloud or a cloud layer). Addressing many scales often requires to use different representations for the different scales, adapted to the apparent size. The second challenge is then to provide seamless shape transitions. This is a very general scientific lock in Computer Graphics and visualization that only few papers address [GPR+03, BPB09].

Scalable illumination models. The appearance of objects results from the incoming light, from the object's reflection properties, and from its shape (responsible for self shadowing). All scales are involved up to microns, but for efficiency reasons we do not want to consider elements smaller than a pixel. We then need to average the illumination contributions of all the subpixel details, up to microns (using one sample per pixel gives aliasing and flickering; using a small number of samples - i.e., oversampling - improves the result but only shifts the problem). Averaging the contributions of micro-scale details ("micro-facets") for surfaces with known statistical properties yields Bidirectional Reflection Distribution Functions (BRDF) models [CT81, Bli82, Kaj85, HTSG91, War92, Sch94, AS00]. But these models are only valid for one scale. At larger scales we need to average the contributions of macroscopic details (e.g., leaves in a tree, trees in a forest), each with its own

BRDF, orientation, incoming light, shadows, etc (which is much more complicated than averaging the shape alone). This is again a hard scientific lock that only few papers address [Fou92, BM93, ON94, TLQ+05, HSRG07, TLQ+08, BNH10].

Computing the outgoing light requires to know the incoming light, which includes the light outgoing from other objects. This leads to global illumination, a field which has been hugely investigated for indoor environments. Still, global illumination remains costly, even when precomputations are used [SKS02]. And global illumination is even more complicated in outdoor environments with very long range interactions. Only few papers addressed this issue for specific cases (terrain [OS07], trees [HPAD06, BBP08], cloud layers [BNL06]) and limited scale. Much work remains to extend this to Earth scale.

Scalable animation models. Our goal is to get water (ocean, rivers) and clouds animated in physically plausible ways, at all scales. Their motion results from physical equations that have been simulated with grids (Eulerian methods like [Sta99, DKY+00]), particles (Lagrangian methods like [PTB+03]), or a mix of the two. The challenge here is again the scalability and the real-time constraint (instabilities due to numerical precision errors have been solved [Sta99], at the price of accuracy and energy dissipation). Eulerian methods can use non uniform grids or multiple grids at different resolutions, which can provide more resolution in regions of interest (finer grid over France for meteorology, near a plane wing for aerodynamic studies). Lagrangian methods, less frequently used, adapt the size and density of particles to their energy, apparent size or location [APKG07]. Despite these techniques, real-time fluid simulations are still limited to small domains. Representing high-resolution evolving clouds in real-time is thus challenging, and doing it in a scalable way is a hard scientific lock.

A possible approach to the problem is to simulate large scale motions by using "macroscopic" physics in addition to the Eulerian and Lagrangian approaches. Indeed large scale phenomena such as river flows, ocean waves and the evolution of air masses can be described with "macrophysics" like hydraulics, wave theory, frontology, etc. Another idea is to use procedural approaches to simulate simple motions and motion details. Some algorithms have been proposed for that [PN01, Che04, BHN07, KTJG08, NSCL08, SB08], but they do not scale to Earth ranges (or address only the largest scale [DYN06]). The challenge is to extend them and to combine seamlessly 2D simulation at global scale, macrophysics at mesoscale (air masses), 3D simulation at cloud scale, procedural details at small scales, etc.

**Our preliminary results** include a scalable shape model for vector-based data on terrains (using procedural techniques to amplify the terrain shape and appearance [BN08b]), a scalable illumination model of the atmosphere, from all viewpoints from ground to space [BN08a], a scalable shape, illumination and animation model of ocean waves in deep ocean [HNC02, BNH10], a scalable animation model of rivers [YNBH09], and some steps towards scalable shape and illumination models for trees and forests [MNP01, DN04, GMN05]. We integrated some of these results [BN08a, BN08b, YNBH09, BNH10] in a prototype Virtual Earth browser called Proland [Pro09] (see Fig. 1). We sold a license of this software to a planetarium company and we use it in an industrial project for flight simulations.



Figure 1: screenshots from our virtual Earth prototype, called Proland

## **2.2. O**BJECTIFS ET CARACTÈRE AMBITIEUX/NOVATEUR DU PROJET / **R**ATIONALE HIGHLIGHTING THE ORIGINALITY AND NOVELTY OF THE PROPOSAL

Our scientific goals are to find representations and algorithms to get real-time and realistic shape, illumination and motion models for natural objects (mainly vegetation, water and clouds) that can be displayed at all scales from centimeters to thousands of kilometers, without visible transitions between scales. We recall again that we do *not* target the best possible physical accuracy as in radiative transfer models or computational fluid dynamics methods (like for instance in remote sensing, climate modelization, meteorology, etc). Instead, we target physical plausibility, i.e., shape, illumination and motion models that look realistic and are efficient enough for real-time applications. This is a different but equally challenging problem.

Although natural elements are part of the research areas of the project's coordinator team (namely the EVASION team at the LJK laboratory), the scalability that we target here is not. Also the other members of the team are either not working on natural elements (e.g. scientific visualization), or on different elements than those targeted here (small animals, humans, etc). Hence our goals in this project are novel and original with respect to the research areas of the LJK laboratory.

These goals are also ambitious, as several scientific locks must be unlocked to reach them. Solving these hard problems, even for some specific cases only, would be important scientific breakthroughs:

- Scalable shape models are hard to design, especially when they must scale on several orders of
  magnitude. And providing seamless transitions between scales greatly complicates the problem. In
  fact these goals have been reached only in few cases, such as terrains [LH04], grass [BPB09] and deep
  ocean [BNH10] (and there are still some limitations, like visible transitions on silhouettes). Vegetation
  models are available for each scale separately (leaf, tree, forest, canopy), and some transitions have
  been investigated (for instance between the leaf and tree scales, and between the tree and forest
  scales), but providing seamless transitions between all scales remains an open problem.
- Scalable illumination models is an even harder problem. Indeed, averaging the shapes inside a pixel is much easier than averaging the illumination contribution of all these shapes, which can have different orientation, visibility (due to self occlusions), lighting (due to self shadowing and inter-reflections) and reflection properties. These problems have been tackled at the micro-scale, yielding BRDF models. The transitions between two scales have been studied in very few papers, generally using simplifying assumptions (for instance by ignoring self-occlusion and/or self shadowing and/or variable reflection properties). Some results are available for sand [TLQ+05] and ocean [BNH10], but scalable illumination models for terrains and vegetation remains an open problem. Scalable global illumination models for outdoor scenes is also an open problem ([BNL06] simulates inter-reflections between clouds and ground, but only for bounded flat terrains).
- Scalable motion models for fluids (water and clouds) is also a hard problem, especially when seamless
  transitions are needed across several orders of magnitude. Although multi-resolution techniques have
  been proposed for grid-based (Eulerian) and particle-based (Lagrangian) methods, providing real-time
  fluid motions on large domains remains difficult. Some methods have been proposed to amplify
  simulation results with noise-based motions [KTJG08, NSCL08, SB08] but they are not real-time.
  Procedural models and macroscopic physical models from hydraulics, wave theory, frontology, etc.
  could be used to simulate large scale motions at low cost, but the challenge is then to combine
  seamlessly 2D simulation at global scale, macrophysics at mesoscale (air masses), 3D simulation at
  cloud scale, procedural details at small scales, etc.

Our expected results are (see Section 3 for details):

- Scalable local illumination models for terrains and vegetation
- Scalable global illumination models for the clouds and terrain inter reflections
- Scalable motion models for ocean waves near shores, potentially including breaking waves
- Scalable motion models for clouds (at least at landscape and Earth scales)

We plan to integrate these results in our existing Virtual Earth prototype, called Proland [Pro09], in order to better spread these results and to increase the technical value of this demonstrator (a software license of the current code base has already been sold to a planetarium company).

# **3. P**ROGRAMME SCIENTIFIQUE ET TECHNIQUE, ORGANISATION DU PROJET / SCIENTIFIC AND TECHNICAL PROGRAMME, PROJECT MANAGEMENT

## **3.1. P**ROGRAMME SCIENTIFIQUE ET STRUCTURATION DU PROJET / SCIENTIFIC PROGRAMME, SPECIFIC AIMS OF THE PROPOSAL

The goal of the project is the real-time unconstrained exploration of a realistic animated Earth from close to far viewpoints. We will only address natural elements: terrain and vegetation, ocean and rivers, clouds and atmosphere. Our preliminary results integrated in the Proland platform [Pro09] already provides some elements. Some of them are mature (scalable terrain, atmosphere rendering, static Earth-scale cloud layer rendering, deep ocean rendering and animation), while others are still very basic (animated rivers, forest models). We will not contribute to the above mature results. Instead, we plan to contribute on four tasks, presented below. We plan to integrate the new results in our prototype Proland, which will also be used as a testbed for new ideas.

Task 1: scalable shape and illumination for terrains, forests and deep ocean. The goal is provide continuous transitions from geometry to normal distributions (NDF) and then to reflectance models (BRDF), in the spirit of what we did in the "simple" case of deep ocean [BNH10]. This case was "simple" because we had an explicit spectral representation of the homogeneous surface, from which we could compute statistical properties for a BRDF. Still, we want to improve the transition quality and the surface spectrum sampling. We then want to apply the same ideas to vegetation, again using statistical properties (here of the distribution of leaves in trees). The problem here is harder because the apparent topology changes with scale (from disconnected leaves to a continuous 2D canopy surface; this requires different representations for the different scales). Finally we want to apply the same ideas to get a scalable terrain illumination model (we already have a scalable shape model). The main problem here is to average self shadows inside a pixel. It is similar to the anti-aliasing of shadowmap-based shadows (averaging the shadow map instead of the shadow test results gives wrong results, since the shadow test is not linear), except that we use horizon maps instead of shadow maps. Note that these "geometry to normals to BRDF transitions" are a very general and hard lock in Computer Graphics, especially when billions of details at the smallest scale project to the same pixel.

Task 2: scalable global illumination between terrain, clouds and atmosphere. The goal is to render in a realistic way the light interactions between the terrain, the clouds and the atmosphere. The Sun and sky light reflected by the terrain illuminates the clouds from below, which reflect this light back towards the ground, and so on. The light is also scattered by the atmosphere as it travels between the ground and the clouds. This gives visible effects like more luminous cloud bottoms above snow (due to its high albedo) and conversely, less luminous cloud bottoms above water (small albedo). Our preliminary work [BNL06] addressed this problem, but was limited to a flat cloud layer, a flat terrain, and a few dozens of kilometers. It was based on symmetry hypotheses that are no longer valid with an arbitrary terrain topography. Extending this work to the Earth scale while taking its topography into account is a challenging task.

Task 3: scalable animated water surfaces. The goal is to animate oceans and rivers in real-time and in a scalable way. Our preliminary work on scalable illumination and animation of the ocean [BNH10] is limited to deep ocean. Coasts and shores appear very unrealistic with this model. Indeed, wave properties change near shores due to depth variations, which cause the reflection and refraction of waves (and the breaking of waves at the shore). Some methods have been proposed to account for reflection and refraction of waves [GS97, GS00] but they rely on long precomputations using wave-tracing. They are not adapted to our needs (users can quickly move from one coast to another). We would also like to improve and extend our scalable real-time river animation model [YNBH09].

Task 4: scalable cloud animation (shape, motion, distribution and evolution). We will first investigate cloud animation at three independent scales: small scale (kilometers), medium scale (dozens of kilometers) and large scale (Earth). We will then work on seamless transitions between them. We do not target exact simulation, but only physical plausibility. At small scale we want to reproduce, in particular, the rising of thermals and cloud puffs, accounting for thermodynamics and phase changes ("small scale" means clouds seen from short distances, *not* a small domain: we want to animate clouds at this scale *anywhere on Earth*). At medium scale we want to reproduce the effects of topography and winds on the distribution and type of clouds. They are influenced by instability patterns (Benard cells, trails, etc). At large scale we want to reproduce the motion of air masses and fronts, resulting from large scale patterns like Rossby waves, Hadley cells, etc. The medium and large scales macrophysical models have never been studied in Computer Graphics, or even in physics (for a global animation model).

### **3.2.** COORDINATION DU PROJET / PROJECT MANAGEMENT

This project involves only two academic researchers of the same laboratory who work in neighbor teams, a PhD student and PostDoc / engineers hired on the project, plus another PhD student and master students (not financed by this project). The project management is therefore trivial. Moreover, tasks and sub-tasks are well separated and independent. A problem in one task will not affect the others. As soon as possible, our results will be integrated into the Proland [Pro09] platform (the first prototypes might be implemented outside this platform), which is managed by Eric Bruneton with the help of engineers (we plan to hire short term engineers on the projet to replace the current ones, whose contracts end in December 2010).

## **3.3.** Description des travaux par tâche / Detailed description of the work organised by tasks

### 3.3.1 TÂCHE 1 / TASK 1

Leader: Eric Bruneton

Participants: Eric Bruneton (18 h.m), PhD student (30 h.m), PostDoc / Engineer (5 h.m), master students

**Goal:** scalable shape and illumination for terrains, forests and deep ocean. The goal is to provide continuous transitions from geometry to normal distributions (NDF) and then to reflectance models (BRDF), in the spirit of what we did in the case of deep ocean [BNH10].

**Subtask 1: scalable shape and illumination of ocean**. Our preliminary work [BNH10] already provides good results, but we want to improve the quality of transitions between scales, as well as the sampling of the surface spectrum. Indeed, we currently build the ocean surface with a finite number of wave trains sampled from the continuous surface spectrum. This can give regular patterns due to wave interferences, which do not look very realistic.

**Subtask 2: scalable illumination of vegetation**. Several shape models are already available to display trees at various scales (from scales at which individual leaves are visible, to the canopy scale). We will therefore not contribute to this aspect. However, there is not currently a corresponding illumination model providing seamless transitions across all these scales. We plan to use the statistical properties of the distribution of leaves inside trees to get a BRDF model of the canopy at large distance. Some models have been proposed by physicists [SS93], but they need to be revisited for real-time rendering. A challenging problem is then the transition between large and small scales, where the number of leaves that project inside a pixel is too large to draw them one by one, but not large enough to use statistical properties. This general problem is complicated here by the fact that the apparent topology changes at the same time (from disconnected leaves to a continuous 2D canopy surface).

**Subtask 3: scalable illumination of terrains**. Unlike the above cases, here we can not rely on statistics to find a BRDF for the terrain seen at large distance (even at these distances, at most a few mountains can project inside a single pixel, not enough to derive statistics). In order to simplify the problem we suppose here that the terrain has a Lambertian BRDF at small scale, and that we can average separately inside a pixel the terrain reflectance and the terrain shadows (i.e., we assume that reflectance and shadows are uncorrelated, which is not always true: snow is more frequently found in shadowed regions). We also ignore inter-reflections and clouds (they are the subject of Task 2). The problem is then "reduced" to find a method to compute the fraction of a pixel that is covered by shadowed terrain parts (ignoring those masked by self-occlusions). We currently use horizon maps (more precisely ambient aperture maps [OS07]) to compute shadows at small scales. The problem is then how to efficiently average the result of several horizon map shadow tests (this is not the same as averaging the horizon map itself, due to non linearities). We plan to extend techniques that have been found to anti-alias shadowmap-based shadows (averaging a shadow map instead of the shadow test results also gives wrong results, since the shadow test is not linear).

### 3.3.2 TÂCHE 2 / TASK 2

Leader: Eric Bruneton Participants: Eric Bruneton (3 h.m), PhD student (6 h.m), PostDoc / Engineer (5 h.m), master students

**Goal:** scalable global illumination between terrain, clouds and atmosphere. The goal is to render in a realistic way the light interactions between the terrain, the clouds and the atmosphere.

Our preliminary work [BNL06] addressed this problem, but was limited to a flat cloud layer, a flat terrain, and a few dozens of kilometers. This removed terrain inter-reflections, and provided symmetries that we used to get an algorithm that did not need any precomputations (it was therefore compatible with cloud animation - task 4), but which was limited to a small domain. In order to extend this work to an arbitrary terrain topography and to the whole Earth, we think that some precomputations are necessary. We hope to be able to

precompute potential terrain inter-reflections (the terrain is not animated), and radiance transfer functions between the terrain and a cloud layer decomposed on some functions basis (we do not want to enforce a specific cloud distribution, in order to allow animation). Also, due to the low altitude of clouds, light interactions between the ground and the clouds remain quite localized, which should allow us to perform tile-based computations during the creation of new terrain and cloud tiles, if necessary, as we did for terrains [BN08b].

### 3.3.3 TÂCHE 3 / TASK 3

#### Leader: Eric Bruneton

Participants: Eric Bruneton (9 h.m), Fabrice Neyret (3 h.m), PhD student (6 h.m), PostDoc / Engineer (5 h.m), master students

Goal: scalable animated water surfaces. The goal is to animate oceans in real-time and in a scalable way.

**Subtask 1: refraction of waves near shores**. Coasts and shores appear very unrealistic with our preliminary work on scalable illumination and animation of the ocean [BNH10], which was limited to deep ocean. Indeed, wave properties change near shores due to depth variations, which cause the reflection and refraction of waves. Some methods have been proposed to account for reflection and refraction of waves [GS97, GS00] but they rely on long precomputations using wave-tracing for a given wind and a given current direction. They are not adapted to our needs (users can quickly move from one coast to another). Instead, we plan to use procedural methods using only local computations (for instance by interpolating potential functions as we did in [YNBH09]) to reproduce the phenomenological effects of wave refraction, such as the progressive alignment of wave fronts with the shore line.

**Subtask 2: breaking waves**. Another missing element in our work [BNH10] for a realistic model at shores is the breaking of waves, due the increase of wave heights, itself due to a decrease of the water depth. Several models have been proposed to render and animate breaking waves, mainly by trying to reproduce the phenomenological aspects of breaking waves (instead of trying to let them emerge from a low level and costly numerical fluid simulation - see for instance [FR86, GS97]). However these models are not adapted to a context where users can quickly move from one shore to another anywhere one Earth. For instance, [MMS04] relies on artist controls to select wave breaking profiles, which is clearly not possible in a large scale context. [TMF+07] relies on a shallow water fluid simulation on a grid, from which wave front lines are extracted to generate breaking waves where necessary. The use of a simulation grid is not adapted to a large domain. We also want to reproduce the phenomenological aspects instead of hoping them to emerge from a numerical fluid simulation, but we want to find plausible models that can be quickly evaluated for any shore anywhere on Earth.

Subtask 3: animated rivers. We want to extend and improve our scalable river animation model [YNBH09].

### 3.3.4 TÂCHE 4 / TASK 4

Leader: Fabrice Neyret

Participants: Fabrice Neyret (15 h.m), Eric Bruneton (6 h.m), PhD student (30 h.m), PostDoc / engineer (3 h.m)

**Goal:** scalable cloud animation (shape, motion, distribution and evolution). We want to investigate cloud animation at three independent scales: small scale (kilometers), medium scale (dozens of kilometers) and large scale (Earth). Here the scale is related to the viewing distance, not to the size of the animated domain: we want to animate clouds at each scale on the whole Earth. We recall that we do not target exact simulation, but only physical plausibility.

**Subtask 1: small scale cloud animation**. Here we only address convective clouds such as cumulus, i.e., those with a well defined and fast evolving shape. A single thermal (or plume, or "puff") rising in a static environment is easy to animate with particle dynamics and thermodynamics laws. However thermals influence each other since they modify their environment, and small thermals can rise in the environment of a big thermal. This suggests a hierarchical model mixing particles and grids, the grids being used to store the environmental conditions and to speed-up the computations of the interactions between neighbor particles. This is a difficult task in the general case, but since we only target plausibility, we can make simplifying assumptions, like only one-way coupling between scales.

In order to animate these thermals anywhere on Earth for ground level views, we plan to use an adaptive representation, to animate only the air parcels that are in the view frustum, at a resolution adapted to their distance to the viewer (in the spirit of [BN08b, YNBH09]). Variations will be provided by varying terrain properties (humidity, temperature, etc), yielding varying thermal emission rates. The main problem is to get a

plausible state for new parcels, when the view changes. We plan to perform a few simulation steps *backward* to recover this state. This is a totally new approach, not expected to be easy. We hope that allowing plausible but not fully accurate animations will simplify the problem (for instance we won't require a cloud to show up at the same place when going back to a previous location).

**Subtask 2: medium scale macrophysical models.** Here we want to reproduce the phenomenological effects of the topography and of the global wind on the motion and distribution of clouds (like cloud channeling in valleys, wind triggered thermals, orographic clouds, hexagonal cloud patterns resulting from Benard cells, cloud stripes resulting from Lee waves, etc). The conditions and characteristics of these patterns are well known, but hoping them to emerge from a numerical fluid simulation is not reasonable, and would not yield controllable results. Instead, we plan to use models inspired from texture synthesis to reproduce these patterns directly where and when they should appear. A reasonable idea is to rely on a 2D cellular automaton with relaxation. It is not expected to be easy since it is a totally new topic.

We also want here to use the phenomenological patterns at the next scale, which are air masses, separated horizontally by front lines. We plan to use as input a vector representation of the front lines (keyframed by an artist, coming from weather forecasts or from a larger scale simulation), and of the macroscopic parameters of air masses and fronts (temperature, humidity, vertical slope, etc), in order to control the previous phenomenological cloud patterns (the formation of clouds at fronts is well understood in meteorology [Vas02, Meteo]).

**Subtask 3: large scale models**. Here we want to reproduce the motion and evolution of high and low pressure areas, which give the air masses and fronts. The atmospheric physics literature [Vas02, Hol04] describes the characteristics and evolution of winds and fronts across them, and also explains the phenomenological patterns at this scale, like Hadley cells (which involve vertical motions), Rossby waves, etc. It is quite easy to simulate highs and lows with a 2D  $\frac{1}{2}$  fluid simulation [DKY+00] taking into account Coriolis forces, where users can specify directly the location and properties of highs and lows, and then let the system simulate their evolution. But it is not so easy to get the phenomenological patterns as emerging properties of this simulation. We might therefore need to find models allowing users to enforce some patterns (which would be a plus anyway for applications with scenarios - games, special effects, flight simulation training).

The risks and difficulties in Task 4 are linked to set of new representations and algorithms to be invented, from the few existing tools in Computer Graphics, or directly from the physics literature. Another problem is to tune the algorithms so that they produce plausible visual phenomena. Our strategy to reproduce the phenomenological patterns directly at each scale, instead of hoping them to emerge from low level fluid simulation is a big advantage here. Note that the models envisioned in this task are independent. Each can be seen as a "fluid amplification" bringing details to the larger model. So, risks are local: beside simulating automatically the whole Earth from ground to satellite scale, the techniques we propose can also be used to visually enrich weather forecast simulations, or to offer high scale handles to control the look of detailed simulation, as expect by scenarists (for games, special effects, flight simulations training).

### **4. A**NNEXES

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